
Fondamenti della Programmazione: Metodi Evoluti

Prof. Enrico Nardelli

Esercitazione 5

Compilation error? Runtime error? (1)

$f(x, y : \text{INTEGER}) : \text{INTEGER}$

do

if ($x // y$) **then**

Integer
division
of x by y

1

else

0

end

end

Compilation error:
integer expression instead
of boolean

Compilation error:
expression instead of
instruction

Compilation error:
expression instead of
instruction

Hand-On

Compilation error? Runtime error? (2)

```
f(x, y : INTEGER): INTEGER  
  do  
    if (False) then  
      Result := x // y  
    end  
    if (x /= 0) then  
      Result := y // x  
    end  
  end
```

Hands-On

Everything is OK
(during both compilation
and runtime)

Calculating function's value

```

f(max : INTEGER; s : STRING): STRING
    do
        if s.is_equal ("Java") then
            Result := "J**a"
        else
            if s.count > max then
                Result := "<an unreadable German word>"
            end
        end
    end
end

```

Hands-On

Calculate the value of:

- $f(3, \text{"Java"}) \rightarrow \text{"J**a"}$
- $f(20, \text{"Immatrikulationsbestätigung"}) \rightarrow \text{"<an unreadable German word>"}$
- $f(6, \text{"Eiffel"}) \rightarrow \text{Void}$

What does this routine do?

```
abs ( $x : REAL$ ):  $REAL$   
  do  
    if ( $x \geq 0$ ) then  
      Result :=  $x$   
    else  
      Result :=  $-x$   
    end  
  end
```

Hands-On

Write a routine...

Hands-On

- ... that increases time by one second inside class *TIME*:

```
class TIME  
    hour, minute, second : INTEGER  
  
    second_forth  
        do ... end  
  
    ...  
  
end
```

Increasing seconds...

```
class TIME
  second_forth
    do
      if second = max_second then
        second := 0
        minute_forth
      else
        second := second + 1
      end
    ensure
      old second = max_second implies second = 0
      old second < max_second implies second = old
      second + 1
    end
  end
```

Increasing minutes... and so on...

```
class TIME
  minute_forth
  do
    if minute = max_minute then
      minute := 0
      hour_forth
    else
      minute := minute + 1
    end
  ensure
    old minute = max_minute implies minute = 0
    old minute < max_minute implies minute = old
    minute + 1
  end
end
```

Simple loop (1)

Hands-On

How many times will the body of the following loop be executed?

i: *INTEGER*

...

from

i := 1

In Eiffel we usually start counting from 1

until

i > 10

10

loop

print (“I will not say bad things about assistants”)

i := *i* + 1

end

Simple loop (2)

Hands-On

And what about this one?

i : *INTEGER*

...

from

i := 10

until

i < 1

loop

print (“I will not say bad things about assistants”)

end

∞

Caution!

Loops can be infinite!

What does this function do?

Hands-On

```
factorial (n : INTEGER): INTEGER
  local
    i : INTEGER
  do
    from
      i := 2
      Result := 1
    until
      i > n
    loop
      Result := Result * i
      i := i + 1
    end
  end
end
```

Loop, **full** form

Syntax:

from

initialization

Instruction

invariant

inv

Optional

until

Boolean expression

exit_condition

Boolean expression

loop

body

Instruction

variant

var

Optional

end

Integer expression

Invariant and variant

Loop invariant (do not mix with class invariant)

- holds after execution of **from** clause and after each execution of **loop** clause
- captures how the loop iteratively solves the problem: e.g. “to calculate the sum of all n elements in a list, on each iteration i ($i = 1..n$) the sum of first i elements is obtained”

Loop variant

- integer expression that is nonnegative after execution of **from** clause and after each execution of **loop** clause and strictly decreases with each iteration
- a loop with a variant can not be infinite (why?)

Invariant and variant

Hands-On

What are the invariant and variant of the “factorial” loop?

from

$i := 2$

Result := 1

invariant

Result = *factorial* ($i - 1$)

until

$i > n$

loop

Result := **Result** * i

$i := i + 1$

variant

$n - i + 1$

end

$i = 4$; **Result** = 6 = 3!

When features are used in contracts, *their* contracts are **NOT** checked

$n - i + 1$
it's enough, if we call
factorial with $n > 0$

Which are the contracts?

require

$n \geq 0$

do

from

$i := 2$

Result := 1

invariant

Result = *factorial* ($i - 1$)

until

$i > n$

loop

Result := **Result** * i

$i := i + 1$

variant

$n - i + 2$

end

ensure

$n > 0$ implies **Result** = n * *factorial* ($n - 1$)

end

LINKABLE (a predefined Eiffel class)

To make it possible to link infinitely many similar elements together, each element should contain a reference to the next element

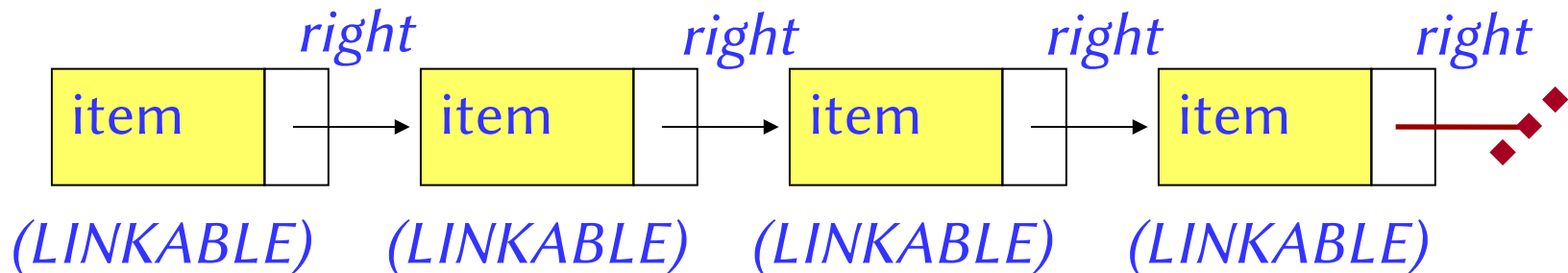
```
class LINKABLE
```

```
  feature
```

```
    ...
```

```
    right : LINKABLE
```

```
end
```



INT_LINKABLE

```

class INT_LINKABLE
create set_value
feature -- Access
    value : INTEGER
    next : detachable INT_LINKABLE
feature -- Initialization
    set_value (a_value : INTEGER)
        do value := a_value
        ensure value = a_value
        end
feature -- Processing
    link_to (other : detachable INT_LINKABLE)
        -- connect to `other`
        do next := other
        ensure next = other
        end
end

```

No need of
requiring
other /= Void

```
class INT_LINKED_LIST
feature -- Access
    first_element : detachable INT_LINKABLE
        -- First element of the list

    last_element : detachable INT_LINKABLE
        -- Last element of the list

    active_element : detachable INT_LINKABLE
        -- Current element of the list

    count : INTEGER
        -- Number of elements in the list
    ...
invariant
    ...
end
```

class *INT_LINKED_LIST*

feature – Cursor movement

start

-- Set `active\_element` to the first element

do

active_element := first_element

ensure *active_element = first_element*

end

last

-- Set `active\_element` to the last element

do

active_element := last_element

ensure *active_element = last_element*

end

forth

-- Set `active\_element` to the next element, if exists

do

if attached *active_element* **as** *ae* **then**

active_element := ae.next

end

ensure attached old *active_element* **as** *ae* **implies** *active_element = ae.next*

end

end

INT_LINKED_LIST class invariant

invariant

count ≥ 0

last_element $\neq \text{Void}$ implies *last_element.next* = **Void**

...

...

...

Is it
Void Safe?

Look here!

end

INT_LINKED_LIST class invariant

invariant

count ≥ 0

attached *last_element* **as** *le* **implies** *le.next* = **Void**

count = 0 **implies**

(*first_element* = *last_element*) **and**

(*first_element* = **Void**) **and**

(*first_element* = *active_element*)

count = 1 **implies**

(*first_element* = *last_element*) **and**

(*first_element* $\neq$ **Void**) **and**

(**attached** *active_element* **as** *ae* **implies** *ae* = *first_element*)

count = 2 **implies**

(*first_element* $\neq$ **Void**) **and**

(*last_element* $\neq$ **Void**) **and**

(**attached** *active_element* **as** *ae* **implies** *ae* = *first_element* **or** *ae* = *last_element*) **and**

(**attached** *first_element* **as** *fe* **implies** *fe.next* = *last_element*)

count > 2 **implies**

(*first_element* $\neq$ *last_element*) **and**

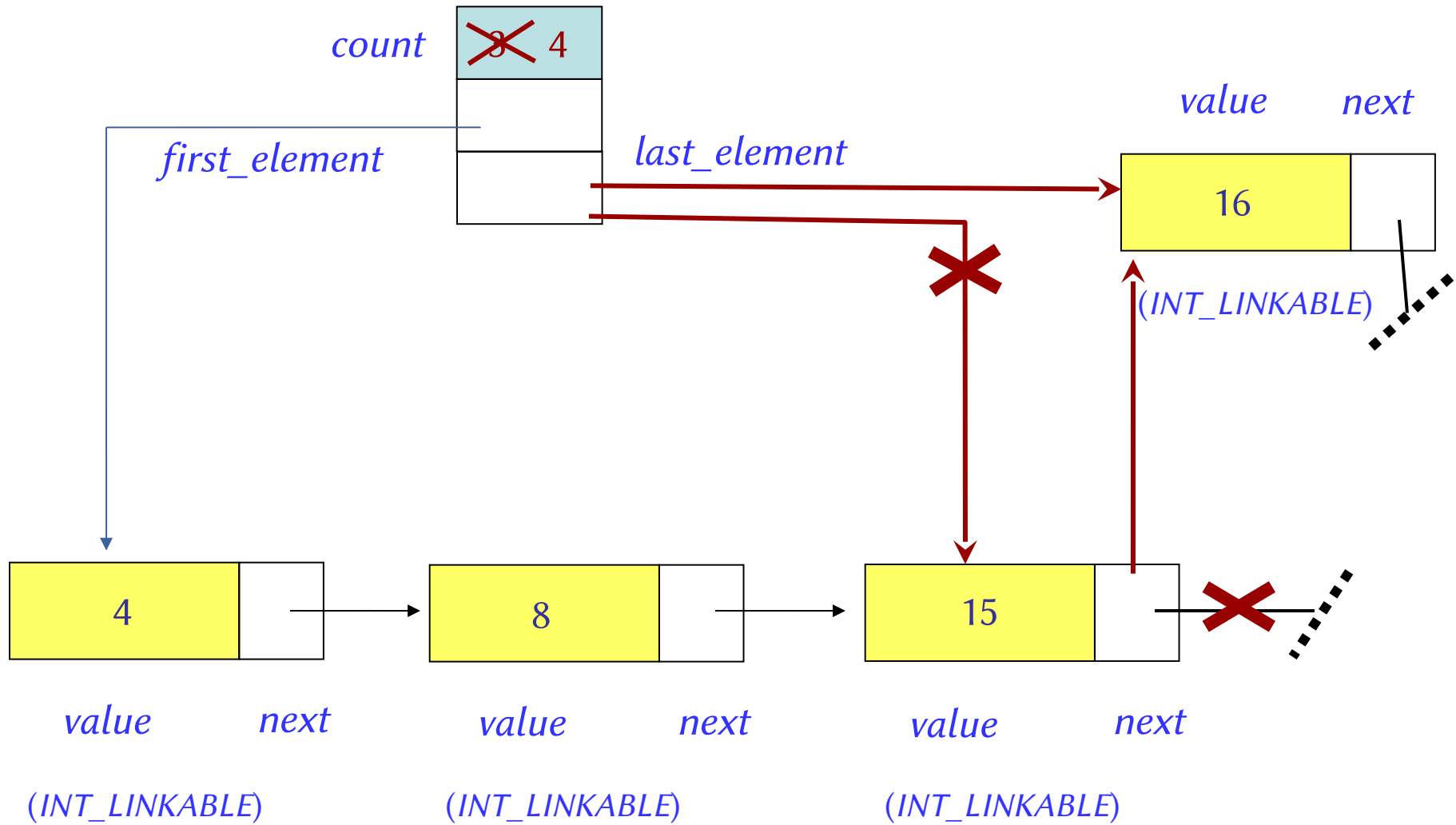
(*first_element* $\neq$ **Void**) **and**

(*last_element* $\neq$ **Void**) **and**

(**attached** *first_element* **as** *fe* **implies** *fe.next* $\neq$ *last_element*)

end

INT_LINKED_LIST: inserting at the end



INT_LINKED_LIST: inserting at the end

```

append(a_value : INTEGER)
  -- Add 'a_value' after 'last_element'.
  local
    new_element: like first_element
  do
    create new_element.set_value(a_value)
    if count = 0 then
      first_element := new_element
    else
      if attached last_element as le then
        le.link_to(new_element)
      end
    end
    last_element := new_element
    count := count + 1
  ensure
    count = old count + 1
    attached last_element as le implies le.value = a_value
    attached old last_element as ole implies ole.next = last_element
  end

```

Is it
Void Safe?

INT_LINKED_LIST: searching for an item

has (a_value: INTEGER): BOOLEAN

-- Does list contain `a\_value`?

For the **variant** contract
k: INTEGER

local

previous_element, current_element : like first_element

do

from

k := 0

current_element := first_element

previous_element := Void

invariant

not Result implies

(previous_element /= Void implies

previous_element.value /= a_value)

Result implies

(previous_element /= Void implies

previous_element.value = a_value)

until

(current_element = Void) or Result

loop

if *current_element.value = a_value* **then**

Result := True

k := k+1

end

previous_element := current_element

current_element := current_element.next

end

end

variant
count - k

Are these calls
Void Safe?

INT_LINKED_LIST: finding an item

get_element (*a_value*: *INTEGER*): detachable *INT_LINKABLE*

-- Return the first element containing '*a_value*', if exists

local

previous_element, *current_element*: like *first_element*

do

from

current_element := *first_element*;

previous_element := Void

invariant

Result = Void implies

(*previous_element* /= Void implies *previous_element.value* /= *a_value*)

Result /= Void implies

(*previous_element* /= Void implies *previous_element.value* = *a_value*)

until

current_element = Void or else *current_element.value* = *a_value*

loop

previous_element := *current_element*

current_element := *current_element.next*

end

Result := *current_element*

ensure

Result /= Void implies **Result.value** = *a_value*

Result = Void implies not *has(a_value)*

end

Are these calls
Void Safe?

For the **variant** contract
introduce the same
changes as in previous
slide



Write a routine that

- inserts value *a_value* after the first occurrence of a value *target* and add *a_value* at the end if the value *target* is not found
- do not reuse in the code existing feature *has* and *get_element* (generally not a good choice!) – but they may be used in contracts

insert_after (*a_value*, *target*: *INTEGER*)
do ... end

INT_LINKED_LIST: insert_after (1)

```

insert_after (a_value, target : INTEGER)
-- Insert `a_value` right after first occurrence of `target`, if exists,
-- otherwise add `a_value` after `last_element`.
local
  current_element, new_element : like first_element
do
  create new_element.set_value (a_value)
  from current_element := first_element
  until current_element = Void or else current_element.value = target
  loop current_element := current_element.next
  end
  if current_element /= Void then
    new_element.link_to (current_element.next)
    current_element.link_to (new_element)
    if current_element = last_element then
      last_element := new_element
    end
  else -- list does not contain `target`
    ...
  end
  count := count + 1
ensure
  count = old count + 1
  not old has(target) implies
    (attached last_element as le implies le.value = a_value)
  old has(target) implies (attached get_element(target) as ge implies
    (attached ge.next as gen implies gen.value = a_value) )
end

```

Refactor into feature
link_after

INT_LINKABLE (final version)

```

class INT_LINKABLE
create set_value
feature -- Access
    value : INTEGER
    next : detachable INT_LINKABLE
feature -- Initialization
    set_value (a_value : INTEGER)
        do value := a_value
        ensure value = a_value
        end
feature -- Processing
    link_to (other : detachable INT_LINKABLE)
        -- Connect to `other`.
        do next := other
        ensure next = other
        end
    link_after (other : INT_LINKABLE)
        -- insert after `other` preserving what was after it.
        do
            link_to (other.next)
            other.link_to (Current)
        ensure
            next = old other.next
            other.next = Current
        end
end
end

```

Same as
next := other.next ?

Yes!

Same as
other.next := Current ?

No!

INT_LINKED_LIST: insert_after (2)

```

insert_after (a_value, target : INTEGER)
-- Insert `a_value` right after first occurrence `target`, if exists,
-- otherwise add `a_value` after `last_element`.
local
    current_element, new_element : like first_element
do
    create new_element.set_value (a_value)
    from current_element := first_element
    until current_element = Void or else current_element.value = target
    loop current_element := current_element.next
    end
    if current_element /= Void then
        new_element.link_after (current_element)
        if current_element = last_element then
            last_element := new_element
        end
    else -- list does not contain `target`
        ...
    end
    count := count + 1
ensure
    count = old count + 1
    not old has(target) implies
        (attached last_element as le implies le.value = a_value)
    old has(target) implies (attached get_element(target) as ge implies
        (attached ge.next as gen implies gen.value = a_value) )
end

```

INT_LINKED_LIST: insert_after (3)

```

insert_after(a_value, target : INTEGER)
-- Insert `a_value` right after first occurrence `target`, if exists,
-- otherwise add `a_value` after `last_element`.
local
    current_element, new_element : like first_element
do
    create new_element.set_value(a_value)
    ...
    if current_element /= Void then
    ...
    else -- list does not contain `target`
        if count = 0 then
            first_element := new_element
        else
            if attached last_element as le then
                new_element.link_after(le)
            end
        end
        last_element := new_element
    end
    count := count + 1
ensure
    ...
end

```

Same as
le.link_to(new_element) ?

Yes!



Write a routine that

- calculates the sum of all positive values in a list

sum_of_positive: INTEGER

do ... end

INT_LINKED_LIST: **sum_of_positive**

sum_of_positive: *INTEGER*

-- The sum of positive elements

local

current_element : **like** *first_element*

do

from

current_element := *first_element*

until

current_element = **Void**

loop

if *current_element.value* > 0 **then**

Result := **Result** + *current_element.value*

end

current_element := *current_element.next*

end

ensure

Result >= 0

end