Proposed solution of problem J648

Let a, b, c be positive real numbers such that ab + bc + ca = 1. Prove that

$$a+b+c+3abc \ge \frac{4}{a+b+c}$$

When does equality hold?