

Proposed solution to problem O689

*Prove that  $5/2$  is the minimum positive value of the constant  $k$  such that*

$$\sqrt{\frac{b+c}{ka+b+c}} + \sqrt{\frac{c+a}{kb+c+a}} + \sqrt{\frac{a+b}{kc+a+b}} \geq 3\sqrt{\frac{2}{k+2}}$$

*holds for any nonnegative real numbers  $a, b, c$  with  $a+b+c > 0$ .*